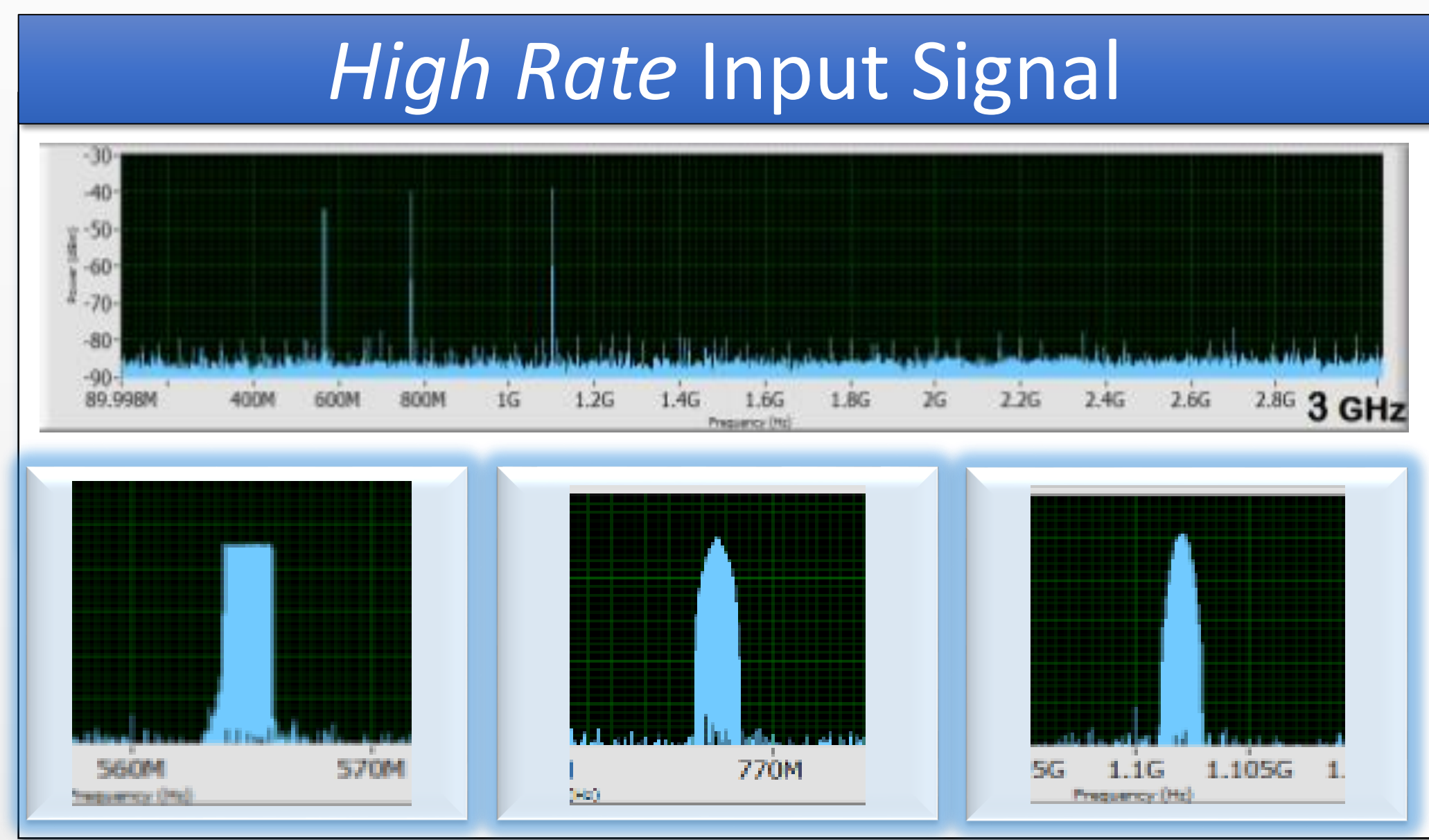
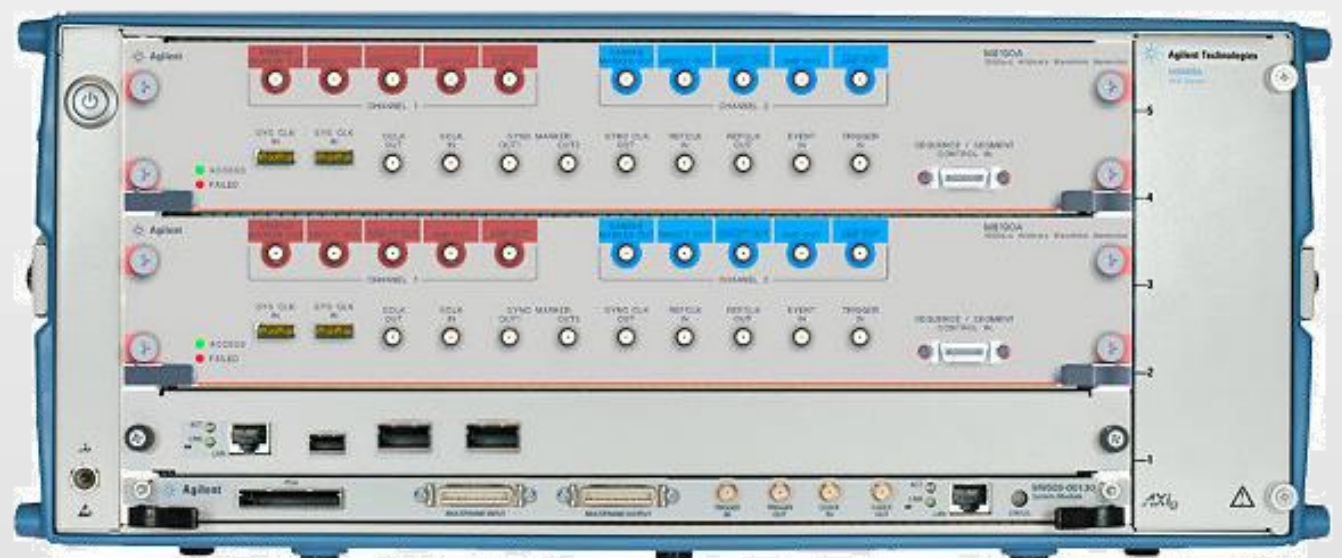


# Sub-Nyquist Cognitive Radio System

Etgar Israeli, Shahar Tsiper, Deborah Cohen, Eli Shoshan, Alex Reysensen, Rolf Hilgendorf, Yonina C. Eldar

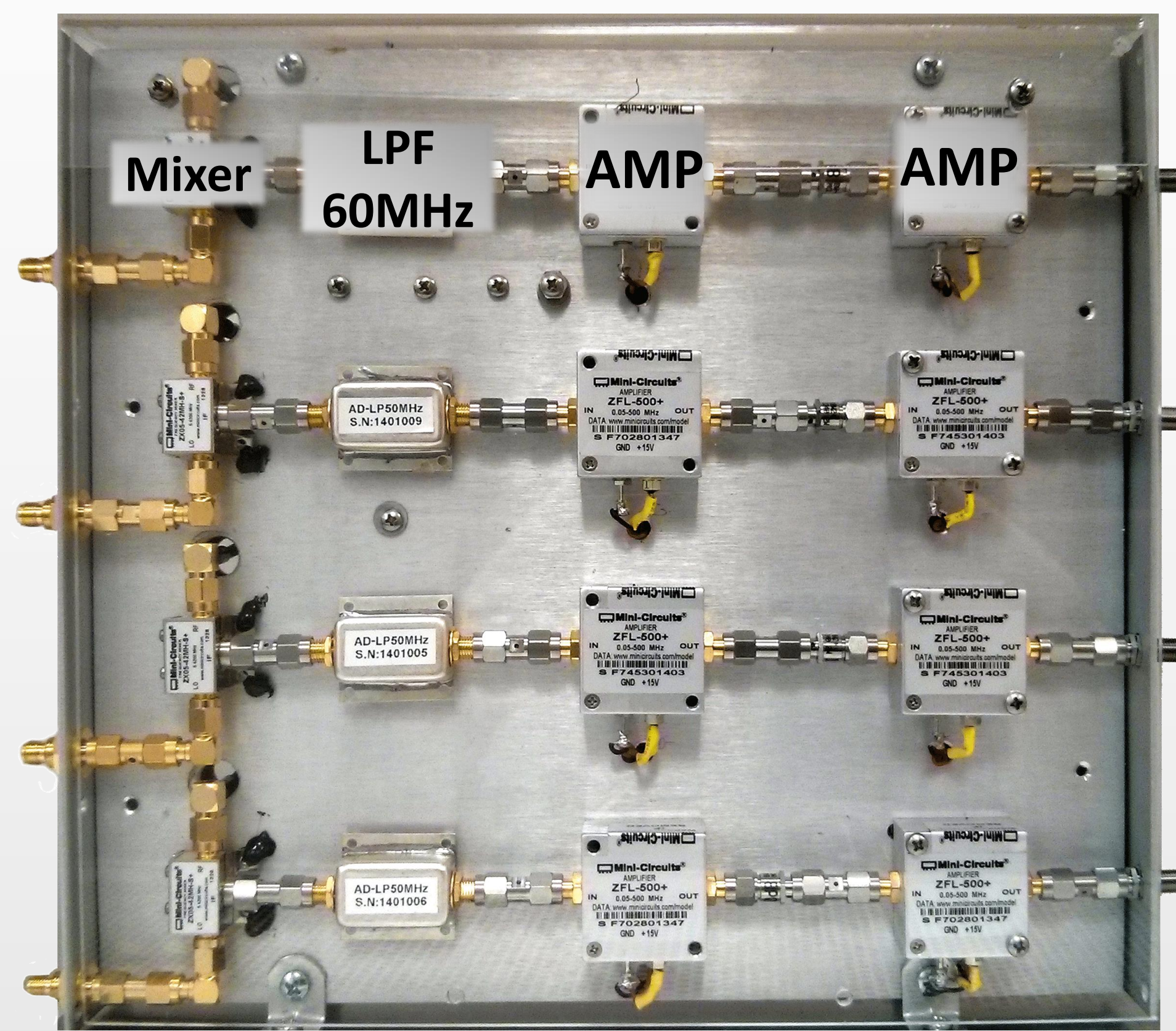


Agilent® Arbitrary Wave Generator M8190

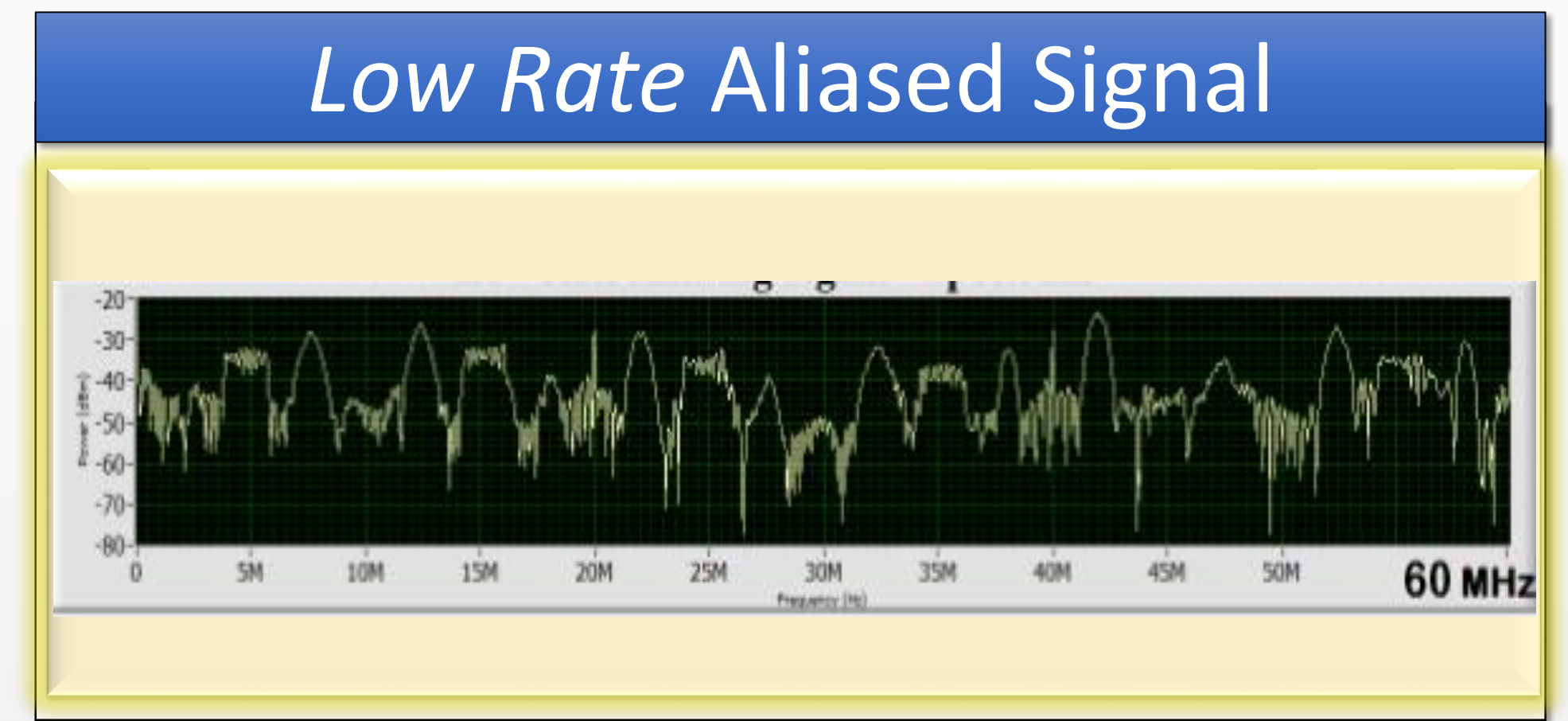


Signal and Sequences Generator

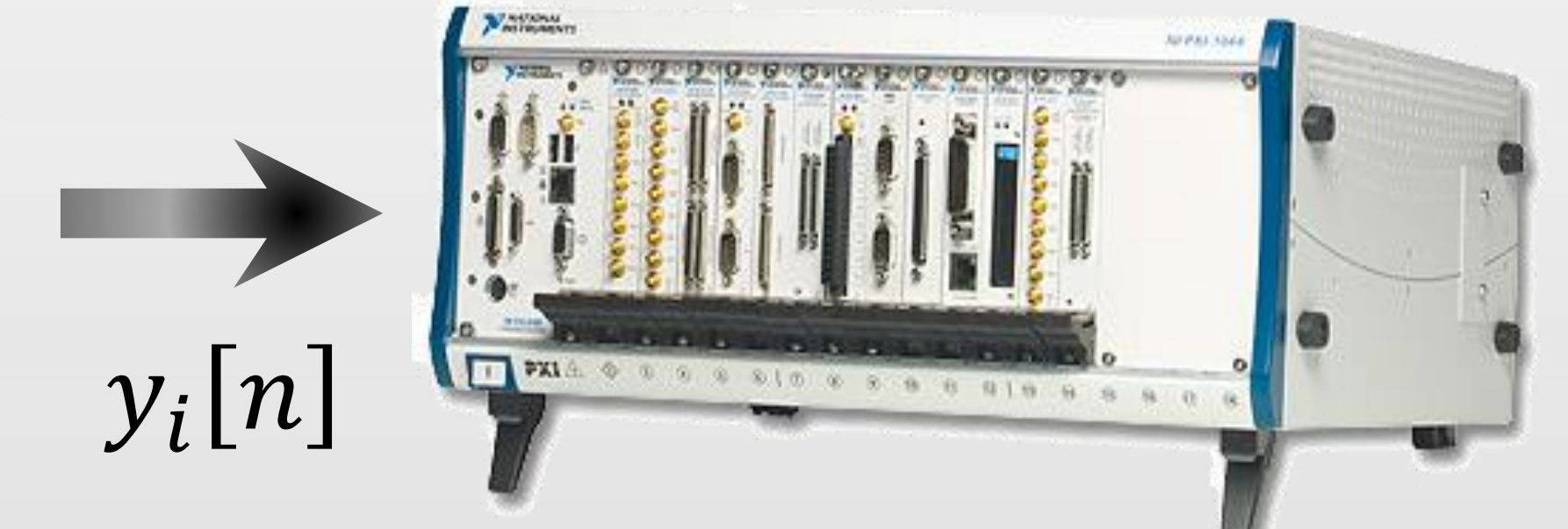
$x(t)$   
 $p_i(t)$



The MWC Card



NI® PXIe-1065 with DC Coupled 4-Channel ADC

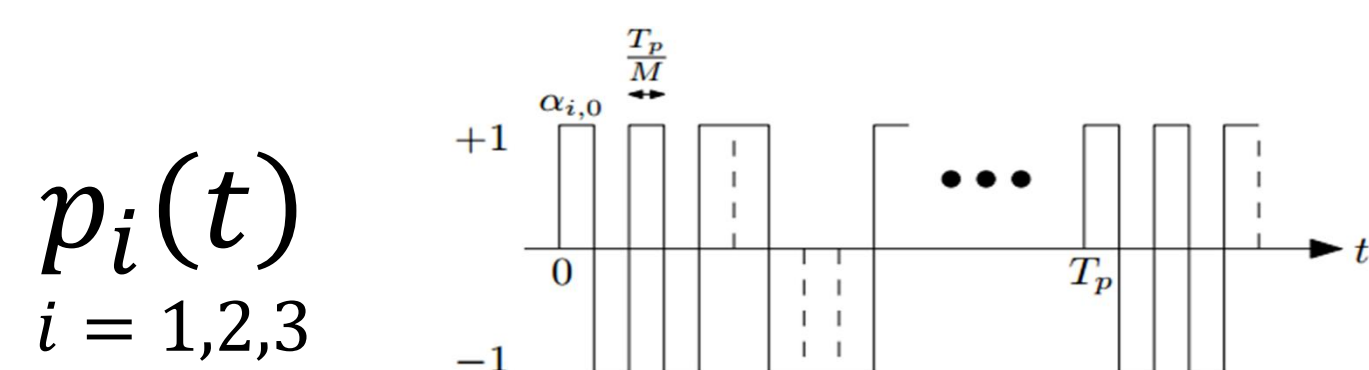


Signal ADC + DSP

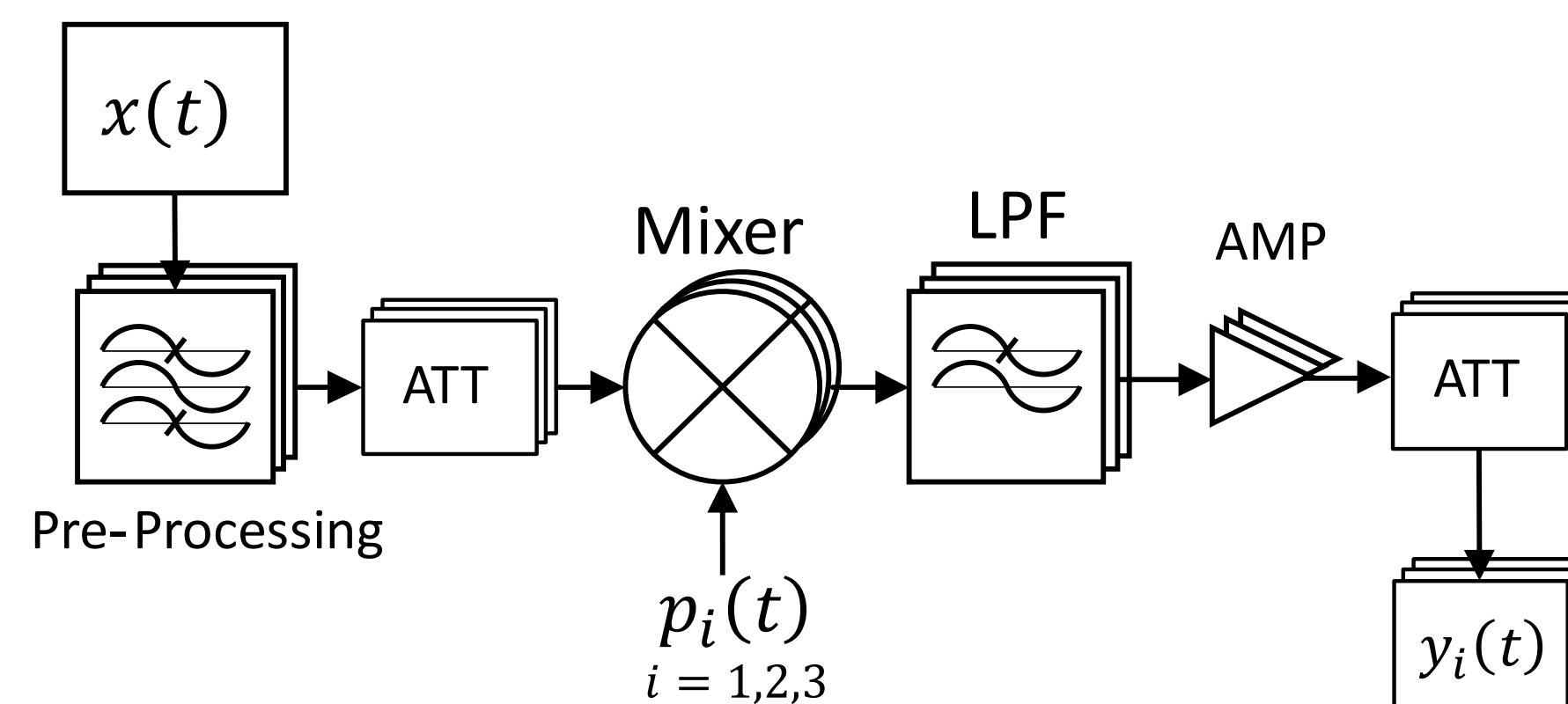
$y_i[n]$

## Mixing Series

- The mixing series are generated at high rate and alias the signal's bands to baseband.
- Alternate between  $\pm 1$  at rate 6.1GHz.
- Generated using Agilent® Arbitrary Wave Generator M8190.

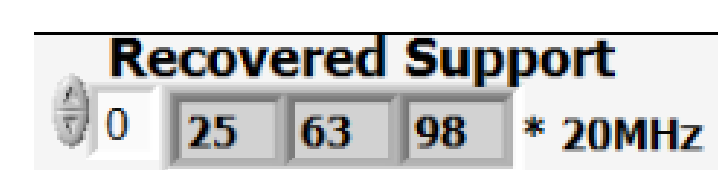


## Analog Design



## Digital Support & Signal Recovery

- The transfer matrix  $\mathbf{A}$  is produced by the calibration procedure.
- The Orthogonal Matching Pursuit (OMP) algorithm is used to detect the transmitted signal carriers.
- the signal slices are then reconstructed by inverting the matrix  $\mathbf{A}$  reduced to the recovered support:
 
$$\mathbf{y}[n] = \mathbf{A}z_s[n] \Rightarrow \hat{z}_s(f) = \mathbf{A}_s^\dagger \mathbf{y}(f)$$
- Support recovery and reconstruction occurs in real time

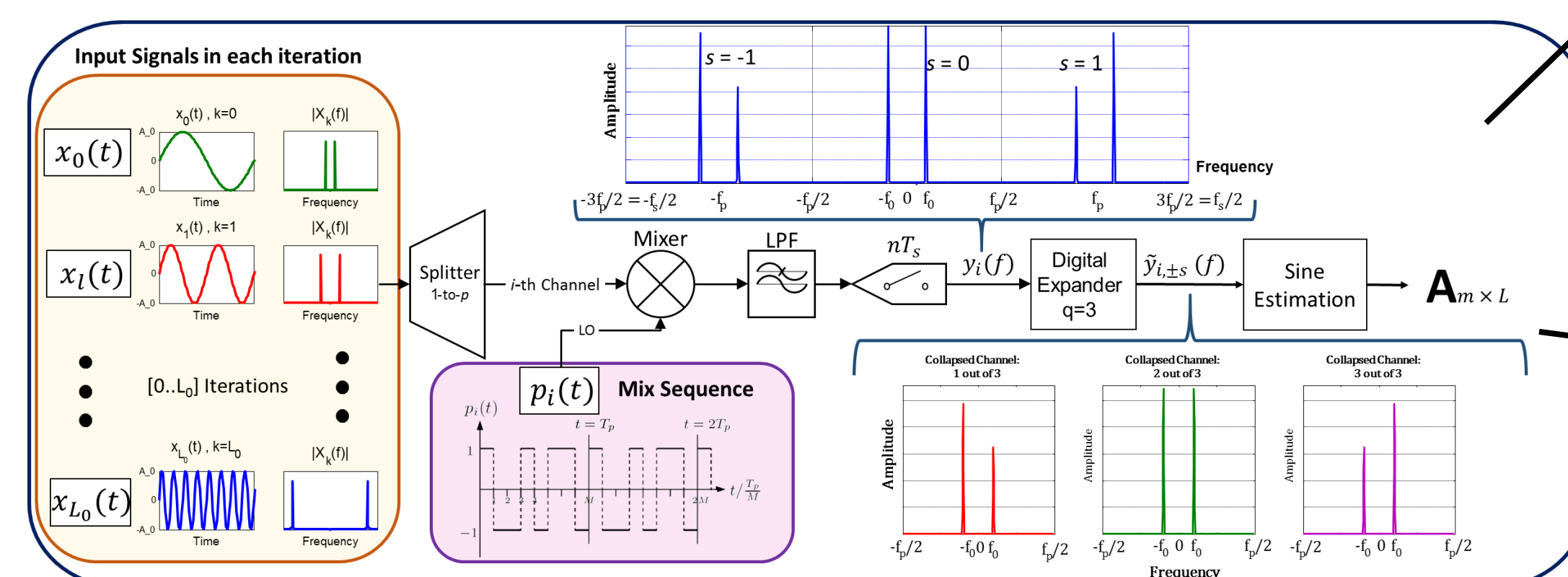


## The Calibration Process

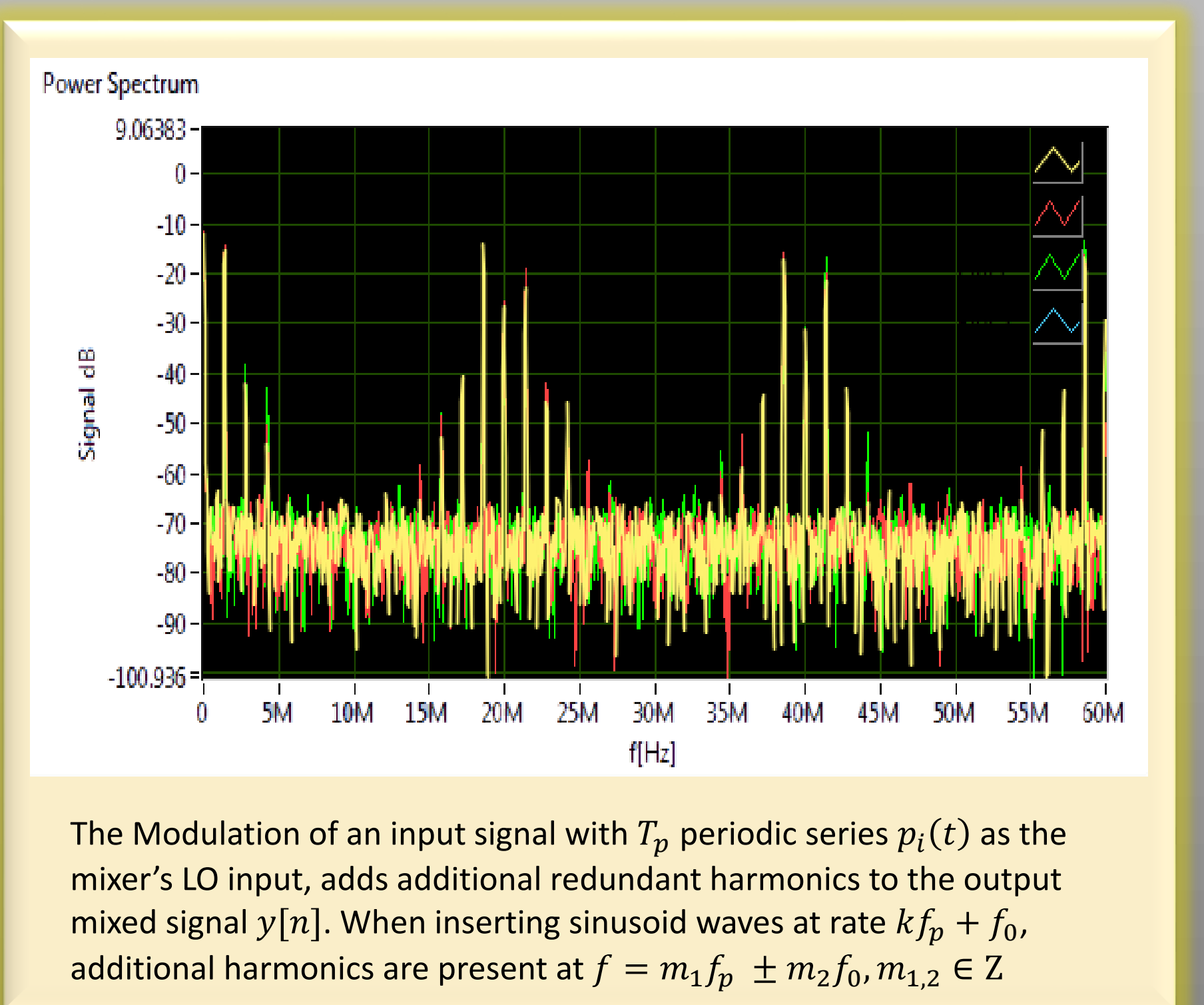
- The calibration process estimates the transfer function of the system, the matrix  $\mathbf{A}$ .
- In the  $l$ -th step, a sine wave is injected to the system:
 
$$x_l(t) = \beta_0 \sin(2\pi f_p l + f_0)$$
- To recover the skewed coefficients of the expander we use linear combinations of the output samples.
- An estimation technique recovers the coefficients of the transfer matrix  $\mathbf{A}$ .

- Least Squares (Trust Region method) minimizes the error according to:

$$[\hat{\beta}_0, \hat{\varphi}_0] = \arg \min_{\beta', \varphi'} \|\tilde{\Psi}_n - \beta' \sin(2\pi \tilde{f}_0 n + \varphi')\|^2$$

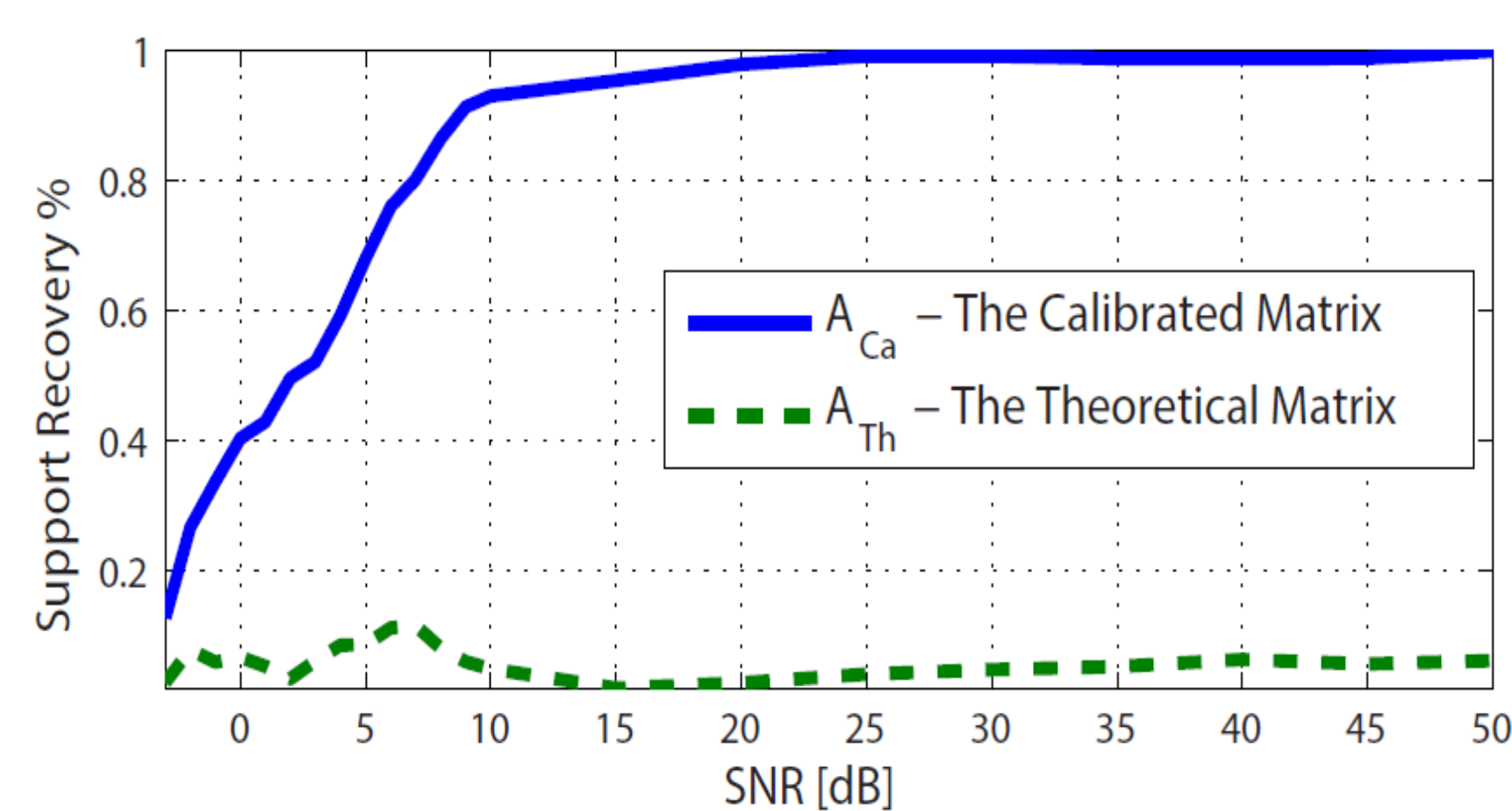


The autonomous calibration process flow chart.

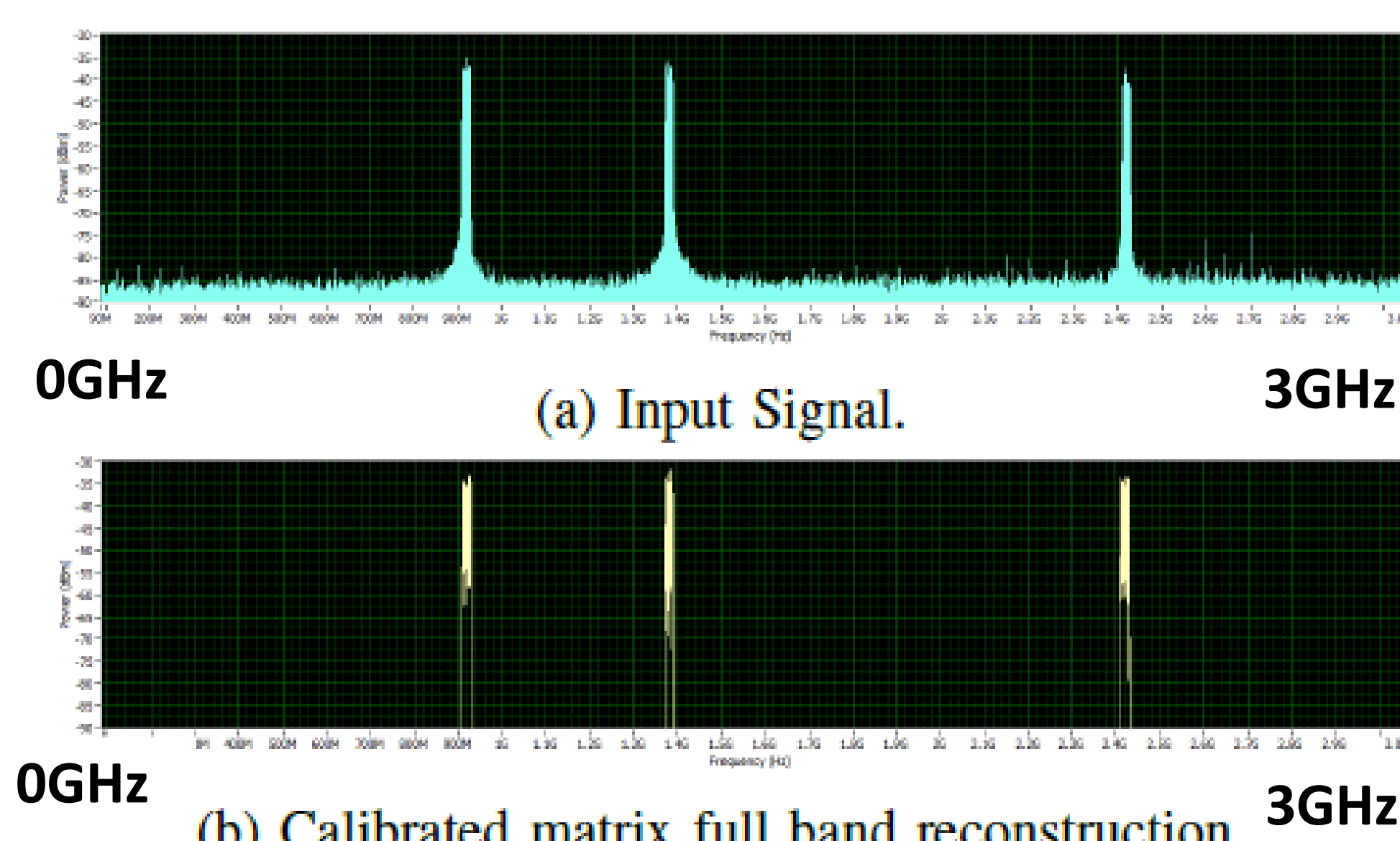


The Modulation of an input signal with  $T_p$  periodic series  $p_i(t)$  as the mixer's LO input, adds additional redundant harmonics to the output mixed signal  $y[n]$ . When inserting sinusoid waves at rate  $kf_p + f_0$ , additional harmonics are present at  $f = m_1 f_p \pm m_2 f_0, m_{1,2} \in \mathbb{Z}$

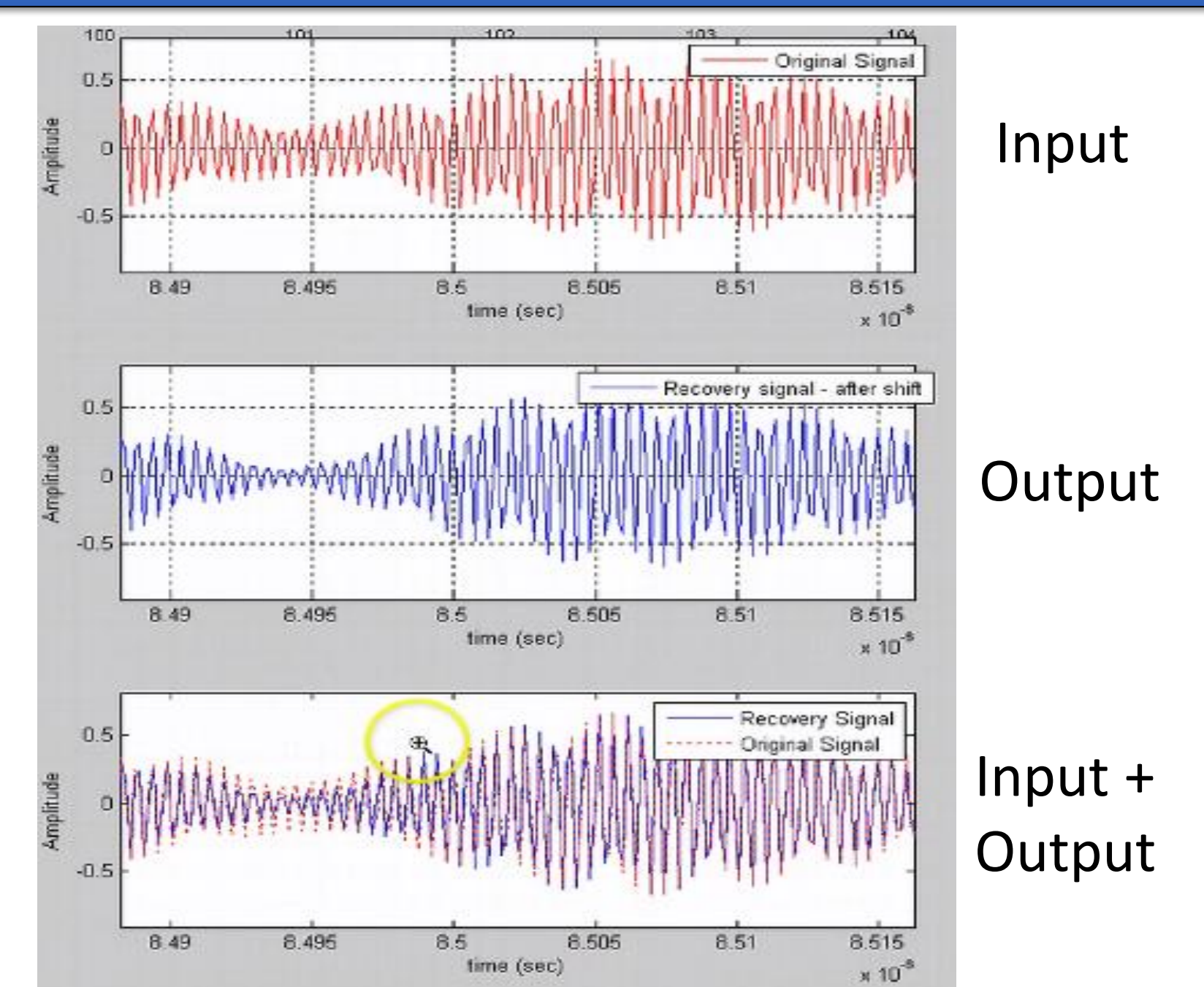
## Results



Hardware reconstruction success percentage of the calibrated matrix  $\mathbf{A}_{calibrated}$  vs. the theoretical  $\mathbf{A}_{Theory}$ .



Correct support detection of the input signal, and full reconstruction, in frequency domain.



Full reconstruction in time domain

## References

- Mishali, M., & Eldar, Y. C. (2010). From theory to practice: Sub-Nyquist sampling of sparse wideband analog signals. *Selected Topics in Signal Processing, IEEE Journal of*, 4(2), 375-391.
- Cordeiro, Carlos, et al. "IEEE 802.22: the first worldwide wireless standard based on cognitive radios." *New Frontiers in Dynamic Spectrum Access Networks, 2005. DySPAN 2005. 2005 First IEEE International Symposium on*. IEEE, 2005.

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